

REVIEW KEY VOCABULARY

For a list of postulates and theorems, see pp. 926–931.

- triangle, p. 217
- scalene, isosceles, equilateral, acute, right, obtuse, equiangular
- interior angles, p. 218
- exterior angles, p. 218
- corollary to a theorem, p. 220
- congruent figures, p. 225
- corresponding parts, p. 225
- right triangle, p. 241
legs, hypotenuse
- flow proof, p. 250
- isosceles triangle, p. 264
legs, vertex angle, base, base angles
- transformation, p. 272
- image, p. 272
- congruence transformation, p. 272
translation, reflection, rotation

VOCABULARY EXERCISES

- Copy and complete: A triangle with three congruent angles is called ? .
- WRITING** Compare vertex angles and base angles.
- WRITING** Describe the difference between isosceles and scalene triangles.
- Sketch an acute scalene triangle. Label its interior angles 1, 2, and 3. Then draw and shade its exterior angles.
- If $\triangle PQR \cong \triangle LMN$, which angles are corresponding angles? Which sides are corresponding sides?

REVIEW EXAMPLES AND EXERCISES

Use the review examples and exercises below to check your understanding of the concepts you have learned in each lesson of Chapter 4.

4.1

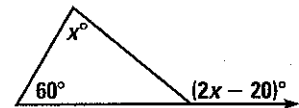
Apply Triangle Sum Properties

pp. 217–224

EXAMPLE

Find the measure of the exterior angle shown.

Use the Exterior Angle Theorem to write and solve an equation to find the value of x .



$$(2x - 20)^\circ = 60^\circ + x^\circ \quad \text{Apply the Exterior Angle Theorem.}$$

$$x = 80 \quad \text{Solve for } x.$$

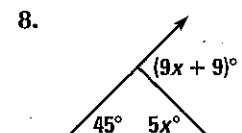
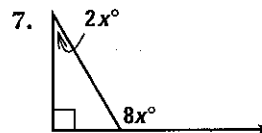
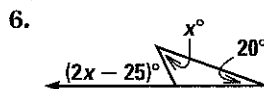
The measure of the exterior angle is $(2 \cdot 80 - 20)^\circ$, or 140° .

EXERCISES

Find the measure of the exterior angle shown.

EXAMPLE 3

on p. 219
for Exs. 6–8



4.2 Apply Congruence and Triangles

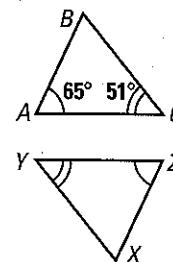
pp. 225–231

EXAMPLE

Use the Third Angles Theorem to find $m\angle X$.

In the diagram, $\angle A \cong \angle Z$ and $\angle C \cong \angle Y$. By the Third Angles Theorem, $\angle B \cong \angle X$. Then by the Triangle Sum Theorem, $m\angle B = 180^\circ - 65^\circ - 51^\circ = 64^\circ$.

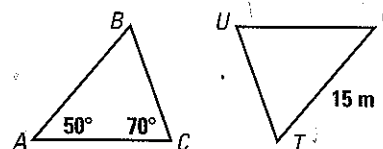
So, $m\angle X = m\angle B = 64^\circ$ by the definition of congruent angles.



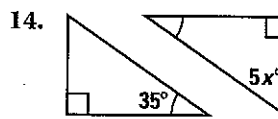
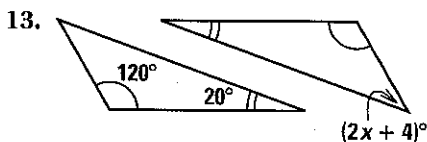
EXERCISES

In the diagram, $\triangle ABC \cong \triangle VTU$. Find the indicated measure.

9. $m\angle B$ 10. AB
11. $m\angle T$ 12. $m\angle V$



Find the value of x .



EXAMPLES 2 and 4
on pp. 226–227
for Exs. 9–14

4.3 Prove Triangles Congruent by SSS

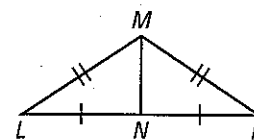
pp. 234–239

EXAMPLE

Prove that $\triangle LMN \cong \triangle PMN$.

The marks on the diagram show that $\overline{LM} \cong \overline{PM}$ and $\overline{LN} \cong \overline{PN}$. By the Reflexive Property, $\overline{MN} \cong \overline{MN}$.

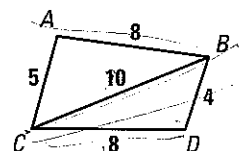
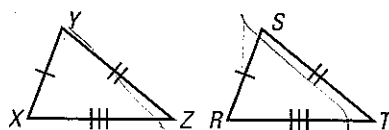
So, by the SSS Congruence Postulate, $\triangle LMN \cong \triangle PMN$.



EXERCISES

Decide whether the congruence statement is true. *Explain* your reasoning.

15. $\triangle XYZ \cong \triangle RST$ 16. $\triangle ABC \cong \triangle DCB$



EXAMPLE 1
on p. 234
for Exs. 15–16

4.4

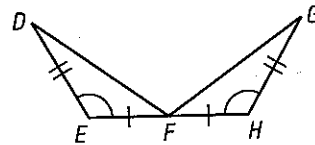
Prove Triangles Congruent by SAS and HL

pp. 240–246

EXAMPLE

Prove that $\triangle DEF \cong \triangle GHF$.

From the diagram, $\overline{DE} \cong \overline{GH}$, $\angle E \cong \angle H$, and $\overline{EF} \cong \overline{HF}$.
By the SAS Congruence Postulate, $\triangle DEF \cong \triangle GHF$.



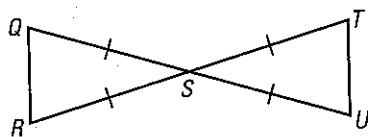
EXAMPLES 1 and 3

on pp. 240, 242
for Exs. 17–18

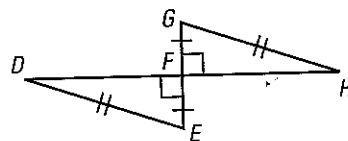
EXERCISES

Decide whether the congruence statement is true. Explain your reasoning.

17. $\triangle QRS \cong \triangle TUS$



18. $\triangle DEF \cong \triangle GHF$



4.5

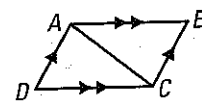
Prove Triangles Congruent by ASA and AAS

pp. 249–255

EXAMPLE

Prove that $\triangle DAC \cong \triangle BCA$.

By the Reflexive Property, $\overline{AC} \cong \overline{AC}$. Because $\overline{AD} \parallel \overline{BC}$ and $\overline{AB} \parallel \overline{DC}$, $\angle DAC \cong \angle BCA$ and $\angle DCA \cong \angle BAC$ by the Alternate Interior Angles Theorem. So, by the ASA Congruence Postulate, $\triangle ADC \cong \triangle CBA$.



EXERCISES

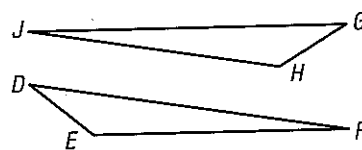
State the third congruence that is needed to prove that $\triangle DEF \cong \triangle GHJ$ using the given postulate or theorem.

19. GIVEN $\triangleright \overline{DE} \cong \overline{GH}$, $\angle D \cong \angle G$, $? \cong ?$

Use the AAS Congruence Theorem.

20. GIVEN $\triangleright \overline{DF} \cong \overline{GJ}$, $\angle F \cong \angle J$, $? \cong ?$

Use the ASA Congruence Postulate.



EXAMPLES 1 and 2

on p. 250
for Exs. 19–20

4.6

Use Congruent Triangles

pp. 256–263

EXAMPLE

GIVEN $\triangleright \overline{FG} \cong \overline{JG}$, $\overline{EG} \cong \overline{HG}$

PROVE $\triangleright \overline{EF} \cong \overline{HJ}$

You are given that $\overline{FG} \cong \overline{JG}$ and $\overline{EG} \cong \overline{HG}$. By the Vertical Angles Congruence Theorem, $\angle FGE \cong \angle JGH$. So, $\triangle FGE \cong \triangle JGH$ by the SAS Congruence Postulate. Corresponding parts of $\cong \triangle$ are \cong , so $\overline{EF} \cong \overline{HJ}$.

